

Hardy Weinberg law

The theory describing the genotypic equilibrium based on stable gene frequencies and random mating is known as the Hardy-Weinberg law. This is the foundation of the realm of population genetics. Its main contribution to evolutionary thought lies in demonstrating that genetic differences in a randomly breeding population tend to remain constant unless acted on by external forces.

Forces -

Historical View → Following the publication of "On the Origin of Species" Darwin proposed that natural selection operated on small continuous hereditary variations while Galton and others maintained that variations were sharp & discontinuous.

The controversy resolved when researches showed that several genes, each with small effect can influence the expression of a single phenotype trait that has a large effect.

By 1930 it was clear that evolution is population phenomenon - that we can interpret as a change in gene frequencies in a population because of the action of various natural forces such as selection and genetic drift and this change can lead to differences among races, species and higher taxonomic levels. Gene frequencies and the gene pool are two major attributes of a population.

Population can be defined as a group of potentially interbreeding organisms. Gene frequency is the ratio of the different alleles of a gene in a population without regards to their homozygosity or heterozygosity. A gene pool consists of all alleles in the gametes of a population and therefore, one represents all the genes available for the next generation.

Hardy - Weinberg - Principle

The conservation of allele (gene) and allele frequencies in large populations under conditions of random mating and in the absence of evolutionary forces, such as selection, migration and genetic drift, which act to change allele frequencies.

At least in 1908 both Hardy in England and Weinberg in Germany disproved the argument against normal Mendelian segregation in population. They demonstrated that gene frequencies do not depend on dominance or recessiveness but remain essentially unchanged from one generation to the next under certain conditions.

The following tables outlines major assumptions and steps in the Hardy - Weinberg - Principle.

Assumptions

(1) Parents represent a random sample of the gene frequencies in the population

(2) Genes segregate normally into gametes

(Heterozygotes) for any gene pair produce their two kinds of gametes in equal frequencies.

(3) Parents are equally fertile (gametes are produced according to the frequencies of the parents)

(4) Gametes are equally fertile (all have an equal chance of becoming a zygote).

(5) The population is very large (all the possible kinds of zygotes will be formed in frequencies determined by the gametic frequencies).

Steps

A. Provide gene frequencies in gametes.

B. Provide gene frequencies in gametes.

C. Provide gene frequency in the gamete that form the zygote.

- (6) Mating between gametes is random
 (not determined by any preferences
 associated with specific genotypes.)
- (7) Gene frequencies are the same
 in both ♂ and ♀ Parents.

B. Provides genotype frequencies in the zygote

- (8) All genotypes have equal reproduction ability

C. Provides genotype frequencies in adult progeny produced by ZV zygote.

F. Repeat at steps A, B, C, E etc.

Populations of Gene Frequencies:

Gene frequencies are simply the proportion of the different alleles of a gene in a population. To get these proportions, we count the total no. of organisms with various genotypes in the population and estimate the relative frequencies of the alleles involved or count the effect on gametes and occasional mutation. The genetic components of all cells in a multicellular organism are the same. We may therefore adopt the convention that a haploid organism has only one gene at any one locus, a diploid has two, a triploid three, and so on.

Examples →

Human's who can and cannot taste the phenylthio carbamide, decides in a single gene. Allelic difference between the alleles T and t. Since the allele for tasting T, is dominant over t, two genotypes (Homozygous TT & Heterozygous Tt) represents tasters and the non-tasters are tt. A population of 300 individuals composed of 90 TT, 60 Tt and 50 tt will there fore have a

Total of 400 alleles at this locus.

TABLE - I

Technique for obtaining gene frequencies from a diploid population of 200 individuals.

(a) Using numerical gene counts (there are 400 genes in 200 diploid individuals)

$$T = 180 (\text{in } TT) + 60 (\text{in } Tt) = \frac{240}{400} = 0.60$$

$$t = 100 (\text{in } tt) + 60 (\text{in } Tt) = \frac{160}{400} = 0.40$$

$$\text{Total} \longrightarrow 1.00$$

(b) Using genotype frequencies: —

$$T = 0.45 TT + \frac{1}{2} (30 Tt) = 0.45 + 0.15 = 0.60$$

$$t = 0.25 tt + \frac{1}{2} (30 Tt) = 0.25 + 0.25 = 0.50$$

$$\text{Total} \longrightarrow 1.00$$

Note \rightarrow these individuals are of the following types \rightarrow

$$90 TT + 60 Tt + 50 tt = 200 \text{ (individuals)}$$

$$0.45 TT + 0.30 Tt + 0.25 tt = 1.00 \text{ (genotypes)}$$

CONSERVATION OF GENE FREQUENCIES: —

The principle Hardy-Weinberg discovered may be simply illustrated using the testing example mentioned above.

Let us, for instance, place on a island a group of children the ratio just given: — 0.45 TT / 0.30 Tt / 0.25 tt

Where gene frequencies are there hence — 0.60 T and 0.40 t

Let us also assume that the no. of individuals in this newly formed population is large and that testing or non-testing has no effect on survival (viability), fertility or attraction between the sexes.

As these children mature, they will choose their mates at random from those of the opposite sex regardless of their tasting abilities. We can then predict mating between any two genotypes solely on the basis of the genotype frequencies in the population. The following table shows nine different types of mating that can occur, of which three are reciprocals of each other.

e.g. $Tt \times Tt = tT \times Tt$

TABLE II

Gene frequencies produced by random mating among individuals in a population having the frequencies given in Table I

$TT = 4.5$ $Tt = 30$ $tt = 2.5$

	$TT = .45$	2025	.1350	.1125
♀	$Tt = .30$	13504	.0900	.0750
	$tt = .25$.1125	.750	.0625

* PARENTS

Mating of genotypes	Box no. from above	mating frequencies	OF spring
		TT	Tt tt
$TT \times TT$	(1)	$= .2025$	0.2025
$TT \times Tt$	(2) + (4)	$= .2700$	$.1350 .1350$
$TT \times tt$	(3) + (7)	$= .2250$	$.2250$
$Tt \times Tt$	(5)	$= .0900$	$.0025 .0450 .0225$
$Tt \times tt$	(6) + (8)	$= .1500$	$0.0750 .0750$
$tt \times tt$	(9)	$= .0625$	$.0625$
Total		$= 1.0000$	$\frac{4200}{3600} = 1.1667$
			$= .1600$

Gene Frequencies among Offspring:

$$T = .25 TT + 1/2 (.45 Tt) = .25 + .15 = .40$$

$$.25 + .15 = .40$$

$$\text{Total} = 1.00$$

Note that the random mating has altered the frequencies of genotypes, the gene frequencies among the offspring have not changed equal to the parent.

Binomial Expansion:

$$(P + Q)^2 = P^2 + 2PQ + Q^2$$

with any given parent

and random mating between genotypes, one generation of a population in which generations do not overlap enough to establish equilibrium has the frequencies of gene and genotypes, once established, the equilibrium will persist until the gene frequencies are changed.

Multinomial Expansion

If there are only three alleles at a locus A_1, A_2, A_3 , with respective frequencies p, q, r so that $p + q + r = 1$. The trinomial expansion $(p + q + r)^2$ determines the genotype equilibrium frequencies.

Independently Assorting Genes

If there are two or more pairs of independently assorting genes, there are many more possible genotypes and the more gene pairs, the longer it will take to achieve overall genotype equilibrium.

Linked Genes

In the case of linkage the higher the frequency of recombination

between linked genes the shorter the time needed to reach equilibrium.

When genes are linked on the X-chromosome, gene frequencies at equilibrium will be equal in both sexes, but this may take a no. of generations if frequencies between the two sexes differ initially.

NATURAL POPULATION →

We can determine genotype frequencies quite easily if no allele is dominant and such observations generally show that equilibrium has been achieved.

If one of the two alleles is dominant, we can get gene frequencies by assuming Hardy-Weinberg equilibrium and using the frequencies of homozygous recessive individuals as q^2 in the genotype equilibrium formula. When we do this for various recessive conditions present in low frequencies the frequency of heterozygous (carriers) is surprisingly high.

CONCLUSIONS:-

Most studies indicate that gene pools are quite stable and generally remain at equilibrium unless selection or some other conditions intervene.

Inbreeding does not affect gene frequencies but does increase homozygosity, allowing selectively rare, recessive alleles to be expressed. If these alleles are harmful, inbreeding depression may result.